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Propagation caracteristics of interaction of chirped vector soliton trains in birefringent optical fibers with variable coefficients in the presence of third and fourth order dispersion and quintic nonlinearity

S. Aziez^{a,b*} and D. Bahloul^a

^aDépartement de Physique, Faculté des Sciences,

Université de Batna, 1 Avenue Boukhlouf Mohamed El Hadi, Batna 05000, Algerie

^bCentre de Recherche Scientifique et Technique en analyse physico-chimique CRAPC, Zone Industrielle lot n°30, Bou Ismail, Tipaza 42415, Algerie

* Corresponding author, email: aziez_siham@hotmail.fr

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Abstract

This paper presents a numerical study of propagation characteristics of chirped vector soliton trains in birefringent optical fibers with variable coefficients. This study is done using the compact split step Padé scheme (CSSPS), in the presence of third and fourth order dispersion and quintic nonlinearity. We are interested in the interaction of adjacent vector solitons in managed birefringent fibers by changing different parameters such us the chirp and the distance between two adjacent vector solitons. In all cases, the energy of each chirped vector soliton remains conserved.

Keywords: Vector soliton trains; Chirped solitons; Birefringent optical fibers; Compact split step Padé scheme; Temporal waveform

1. Introduction

Since the first observation of optical soliton in fused silica fibers by Hasegawa and Tappert [1,2] in 1973, it has demonstrated a big interest because of its possibility to propagate through considerable distances without distortion. Since then, a lot of theoretical and experimental work has been done on the optical soliton propagation in optical fibers [1-20]. In single mode fibers, the pulse propagation in a nonlinear optical fiber can be described by the nonlinear Schrödinger (NLS) equation [1,2,3].

In optical fibers, birefringence is a natural phenomenon that takes place because of effects due to different elements such as curves, turns and anisotropic stress of fibers due to bending [20]. These effects lead up to differential group delay.

Menyuk is the first which has studied the effect of birefringence on the pulse propagation in optical fiber [16]. He predicted that optical vector solitons can be stable under certain operating conditions [17,18]. The two orthogonal polarization modes of the fiber can be coupled together through nonlinear effects leading to cross phase modulation. The propagation of vector solitons in birefringent fibers is governed by a system of two coupled nonlinear Schrödinger (CNLS) equations. The CNLS equations have been the subject of concentrated theoretical, experimental and numerical investigations during recent years [1,2].



Optical vector solitons [1,2] have a rich nonlinear dynamics due to their wide range of applications in fiberoptic-based communication systems [9], and their multicomponent structure [4].

In general, adjacent scalar solitons can interact with each other in dispersion managed fibers leading to rich dynamics, see for example reference [19]. The birefringence in fibers affects significantly the attractive force and leads to collisions of two in-phase solitons in isotropic fibers [21]. In this study, we are interested in the interaction of adjacent vector solitons in managed birefringent fibers. The propagation of vector solitons in managed birefringent optical fibers is governed by the two coupled NLS equations [1,2,4,6,8] with variable coefficients [13]. This kind of equations is not integrable except in few particular cases. We use the numerical compact split step Padé scheme (CSSPS) [5] to investigate the interaction of vector solitons by changing different parameters such us the chirp and the distance between two adjacent vector solitons.

This paper is organized as follows. In Section 2, the coupled nonlinear Schrödinger (CNLS) equations with variable coefficients are mentioned in the presence of third and fourth order dispersion and quintic nonlinearity [10,11,12,14]. In Section 3, we present our numerical model and set the initial conditions with linear chirp. Results and discussions are shown in Section 4.

2. Theoretical model

Managed vector solitons are governed by the coupled nonlinear Schrödinger (CNLS) equations with variable coefficients [1,2,4,5,6,8]:

$$\frac{\partial}{\partial z} \begin{pmatrix} u \\ v \end{pmatrix} + \delta \begin{pmatrix} 1 & 0 \\ 0 & -1 \end{pmatrix} \frac{\partial}{\partial t} \begin{pmatrix} u \\ v \end{pmatrix} + \frac{i}{2} d(z) \frac{\partial^2}{\partial t^2} \begin{pmatrix} u \\ v \end{pmatrix} - i \sum_{n=3}^{n=4} \frac{i^n}{n!} \beta_n \frac{\partial^n}{\partial t^n} \begin{pmatrix} u \\ v \end{pmatrix} + \Gamma(z) \begin{pmatrix} u \\ v \end{pmatrix} = i \gamma(z) \begin{pmatrix} |u|^2 + \varepsilon |v|^2 & 0 \\ 0 & \varepsilon |u|^2 + |v|^2 \end{pmatrix} \begin{pmatrix} u \\ v \end{pmatrix} + i k \begin{pmatrix} |u|^4 + \epsilon |v|^4 & 0 \\ 0 & \epsilon |u|^4 + |v|^4 \end{pmatrix} \begin{pmatrix} u \\ v \end{pmatrix}, \quad (1)$$

Where u(z, t) and v(z, t) are the slowly varying amplitudes of the two polarization modes in the fiber. zand t are respectively the normalized distance and time. δ is the difference of the group velocities between the two polarization components. ε is the cross-phase modulation (XPM) coefficient. For linearly birefringent fibers, $\varepsilon = 2/3$. k is the quintic nonlinearity coefficient. β_3 and β_4 are respectively the third and fourth order dispersion. The functions d(z), $\gamma(z)$ and $\Gamma(z)$ are respectively the managed group velocity dispersion (GVD), the managed self-phase modulation (SPM) and gain (or loss), They are given by the following expressions[7]:

• the varying GVD parameter

$$d(z) = \exp(\sigma z) \gamma(z)/d_0, \qquad (2)$$

• the nonlinear parameter

$$\gamma(z) = \gamma_0 + \gamma_1 \sin(gz), \tag{3}$$

• and the gain (or loss) distributed parameter

$$\Gamma(z) = \sigma / 2, \tag{4}$$

Where d_0 is a parameter related to the initial peak power, σ is a parameter describing gain or loss, and γ_0 , γ_1 and g are the parameters describing Kerr nonlinearity. For our study, we take the parameters $d_0 = 1$, $\gamma_0 = 0$, $\gamma_1 = 1$, g = 1 and $\sigma = 0$ [7].

3. Initial condition

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In order to do our numerical simulations, we choose the following initial conditions [7]:

$$u(0,t) = \cos\alpha \exp(-iCt^2/2)/\cosh(t), \qquad (5)$$

 $v(0,t) = \sin\alpha \exp(-iCt^2/2)/\cosh(t),$ (6) Where, *C* is the linear chirp parameter and the angle α representing the polarization angle.

4. Results and discussions

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In this section, we will be interested in the interaction of adjacent vector solitons in managed birefringent fibers. But first, let us find the shape of the envelope of the scalar soliton in the absence of any perturbation in section 4. 1 with $\alpha = 0^{\circ}$.

Then, when $\alpha = 45^{\circ}$, the two polarization components of a vector soliton have the same amplitude. The section 4.2 addresses the propagation of chirped vector soliton in a managed optical fiber and their interaction in the presence of third and fourth order dispersion and quintic nonlinearity.

4.1. First case: $\alpha = 0^{\circ}$

When $\alpha = 0^{\circ}$, this is the case of an optical soliton with a polarization parallel to the fiber axis. Scalar optical solitons have played an important role in the field of highbit data transmission systems because of the unique properties. They can propagate over long distances keeping their shape unchanged. This property is due to the balance between the dispersion and the nonlinear effects.

Fig. 1 shows the propagation of optical soliton in the absence of any perturbation. As it is well known, optical soliton maintains its shape undistorted.

When we take into account the chirp, we can note that a negative chirp makes the soliton broadening, while; a positive chirp leads to a soliton compression (Fig. 2).



Figure 1. Evolution of unchirped scalar soliton in managed optical fiber with the parameters $\alpha = 0^{\circ}$, C = 0 and $\sigma = 0$



Figure 2. Evolution of chirped scalar soliton in managed optical fiber with the parameters $\alpha = 0^{\circ}$, and $\sigma = 0$: (a) with C = -0.2, and (b) with C = 0.2

4.2. Second case: $\alpha = 45^{\circ}$

In the following three cases, we examine the evolution of vector soliton trains in a managed optical fiber under the effect of the chirp, the quintic nonlinearity, the third and fourth order dispersion when $\alpha = 45^{\circ}$ (the two polarization components have the same amplitude).

4.2.1. Chirped vector soliton in a managed optical fiber

First, we begin with the simple case where we will examine the evolution of vector soliton in a managed optical fiber, under the effect of the chirp. The profile of the intensity of the two polarization components of chirped vector soliton in managed optical fiber are depicted in Fig. 3 (C < 0) and Fig. 4 (C > 0). As in the case of scalar chirped soliton, a negative chirp leads to the optical vector soliton broadening (Fig. 3), while; a positive chirp leads to a vector soliton compression (Fig. 4) with the increase of propagation distance.

To study the effect of third order dispersion alone, β_4 and *k* are set to zero in equation (1). Fig. 5 shows the evolution of the two polarization components of the chirped vector soliton in a managed optical fiber for the following parameters: $\alpha = 45^\circ$, C = 0.2, $\beta_3 = 1$, $\beta_4 = 0$, k = 0 and $\sigma = 0$.

We note that the pulse width of the two polarization components of the chirped vector soliton in a managed optical fiber increases along the propagation distance. At the same time, there is an asymmetric oscillation on the

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trailing edge and a shift of the center of the two polarization components of the chirped vector soliton.

The evolution of the two polarization components of the chirped vector soliton in a managed optical fiber under the effect of fourth order dispersion is studied for the following parameters $\alpha = 45^{\circ}$, C = 0.2, $\beta_3 = 0$, k = 0and $\sigma = 0$. From the plots, we found that a higher value of fourth order dispersion broadens the pulse width as shown in Fig. 6 with the parameter $\beta_4 = 0.08$, and lower values of the same reduce the pulse width us shown in Fig. 7 with the parameter $\beta_4 = 0.01$, which, in turn, will be practical in optical communications.

From Fig. 8 with the parameters $\alpha = 45^{\circ}$, C = 0.2, $\beta_3 = 0$, $\beta_4 = 0$, k = -0.05 and $\sigma = 0$, it is clear that the role of quintic nonlinearity on the propagation characteristics of the two polarization components of the chirped vector soliton in a managed optical fiber is unimportant.

We study now the propagation of the two polarization components of chirped vector soliton in birefringent optical fiber under the combined action of third order dispersion, the fourth order dispersion and the quintic nonlinearity. We note that, in addition to the asymmetric oscillation on the trailing edge, the increase of the pulse width and the shift of the center of the two polarization components of chirped vector soliton along the propagation distance; there is also an oscillation in the amplitude (maximum) of the two polarization components of the chirped vector soliton in a managed optical fiber (Fig.9).





Figure 3. Evolution of the two polarization components of chirped vector soliton in birefringent managed optical fiber with the parameters $\alpha = 45^{\circ}$, C = -0.2 and $\sigma = 0$



Figure 4. Evolution of the two polarization components of chirped vector soliton in birefringent managed optical fiber with the parameters $\alpha = 45^{\circ}$, C = 0.2 and $\sigma = 0$



Figure 5. Evolution of the two polarization components of chirped vector soliton in birefringent managed optical fiber with the parameters $\alpha = 45^{\circ}$, C = 0.2, $\beta_3 = 1$, $\beta_4 = 0$, k = 0 and $\sigma = 0$





Figure 6. Evolution of the two polarization components of chirped vector soliton in birefringent managed optical fiber with the parameters $\alpha = 45^{\circ}$, C = 0.2, $\beta_3 = 0$, $\beta_4 = 0.08$, k = 0 and $\sigma = 0$



Figure 7. Evolution of the two polarization components of chirped vector soliton in birefringent managed optical fiber with the parameters $\alpha = 45^{\circ}$, C = 0.2, $\beta_3 = 0$, $\beta_4 = 0.01$, k = 0 and $\sigma = 0$



Figure 8. Evolution of the two polarization components of chirped vector soliton in birefringent managed optical fiber with the parameters $\alpha = 45^{\circ}, C = 0.2, \beta_3 = 0, \beta_4 = 0, k = -0.05$ and $\sigma = 0$





Figure 9. Evolution of the two polarization components of chirped vector soliton in birefringent managed optical fiber with the parameters $\alpha = 45^\circ$, C = -0.2, $\beta_3 = 1$, $\beta_4 = 0.01$, k = -0.05 and $\sigma = 0$

4.2.2. Interaction between two chirped vector solitons in a managed optical fiber

In this case, we examine the effect of the chirp C and the distance d between two adjacent vector solitons on the interaction between two vector solitons in managed optical fibers.

Whatever the value of the distance d, a negative chirp makes an increase of the amplitude with a decrease of the width of the first vector soliton, while the inverse happens for the second one. A positive chirp makes a decrease of the amplitude with an increase of the width of the first vector soliton, while the inverse happens for the second one. This case is the inverse of the one with a negative chirp. In the case of C = 0, the propagation of the two components of interaction of two vector solitons in birefringent optical fiber is affected by the variation of the distance between two adjacent vector solitons. We note a decrease of the amplitude with an increase of the width of the two polarization components of interaction of two unchirped vector solitons in birefringent optical fiber.

If we take d = 4, we note from Fig. 10, Fig.11 and Fig. 12 that the propagation of two polarization components of interaction of two vector solitons in birefringent optical fiber is affected by the presence of the chirp. If we decrease the distance between two vector solitons (d = 2), we note in Fig. 13, some oscillations between the two vector solitons. This oscillations increase with the decrease of the distance d like in Fig. 14 with d = 1.



Figure 10. Evolution of the two polarization components of interaction of two unchirped vector solitons in birefringent optical fiber with the parameters $\alpha = 45^\circ$, C = 0, $\sigma = 0$, and d = 4





Figure 11. Evolution of the two polarization components of interaction of two chirped vector solitons in birefringent optical fiber with the parameters $\alpha = 45^\circ$, C = -0.2, $\sigma = 0$, and d = 4



Figure 12. Evolution of the two polarization components of interaction of two chirped vector solitons in birefringent optical fiber with the parameters $\alpha = 45^{\circ}$, C = 0.2, $\sigma = 0$, and d = 4



Figure 13. Evolution of the two polarization components of interaction of two chirped vector solitons in birefringent optical fiber with the parameters $\alpha = 45^\circ$, C = -0.2, $\sigma = 0$, and d = 2





Figure 14. Evolution of the two polarization components of interaction of two chirped vector solitons in birefringent optical fiber with the parameters $\alpha = 45^{\circ}$, C = 0.2, $\sigma = 0$, and d = 1

4.2.3. Interaction between three chirped vector solitons in a managed optical fiber

In this section, we examine the effect of the chirp C and the distance d between two adjacent vector solitons d on the propagation of the interaction between three vector solitons in managed optical fibers.

In the case of negative chirp, we note from Fig. 15 an increase in the amplitude and a decrease of the width of the second vector soliton, while the inverse is happen to the first and third ones. In figure 16, a positive chirp makes a decrease of the amplitude with an increase of the width of the second vector soliton, while the inverse happens for the first and third ones. This case is the inverse of the one with negative chirp (Figure 15). In all this cases the energy of each soliton is conserved.

5. Conclusion

In this paper, the propagation characteristics of chirped vector solitons trains in managed birefringent optical fibers are studied numerically. This study is done using the compact split step Padé scheme (CSSPS). The propagation of vector solitons has a rich dynamics. A negative chirp makes the chirped vector soliton broadening, while; a positive chirp leads to a chirped vector soliton compression. From plot, it is clearly noted that, the quintic nonlinearity has a marginal role on the propagation characteristics of the two components of the chirped vector soliton. The evolution of chirped vector soliton trains in managed optical fiber is submitted not only to the presence of the effect of chirp, but also to the interaction between the adjacent vector solitons. In all cases, the energy of each chirped vector soliton remains conserved.



Figure 15. Evolution of the two polarization components of interaction of three chirped vector solitons in birefringent optical fiber with the parameters $\alpha = 45^{\circ}$, C = -0.2, $\sigma = 0$, and d = 2





Figure 16. Evolution of the two c polarization components of interaction of three chirped vector solitons in birefringent optical fiber with the parameters $\alpha = 45^\circ$, C = 0.2, $\sigma = 0$, and d = 2

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References

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- Govind Agrawal, Nonlinear Fiber Optics, Academic Press, fourth edition., US (2007)
- [2] A. Hasegawa and Y. Kodama, Solitons in Optical Communications, Clarendon Press, Oxford, US (1995)
- [3] A. Hasegawa, Theory of information transfer in optical fibers, a tutorial review, Optical Fiber Technology 10, (2004) 50-170
- [4] Darren Rand, Ivan Glesk, Camille-Sophie Brès, Daniel A. Nolan, Xin Chen, Joohyun Koh, Jason W. Fleischer, Ken Steiglitz and Paul R. Prucnal, Observation of Temporal Vector Soliton Propagation and Collision in Birefringent Fiber, Physical Review Letters 98, 053902 (2007)
- [5] Moussa Smadi and Derradji Bahloul, A compact split step Padé scheme for higher-order nonlinear Schrödinger equation (HNLS) with power law nonlinearity and fourth order dispersion, Comput. Phys. Commun. 182, (2011) 366–371
- [6] Siham Aziez, Moussa Smadi and Derradji Bahloul, Semi-Implicit Operator Splitting Padé Method for Vector HNLS Solitons, AIP Conference Proceedings, 1047 (1). DOI:10.1063/1.2999940, (2008)
- [7] Hongjun Zheng, Chongqing Wu, Zhi Wang, Huishan Yu, Shanliang Liu and Xin Li, Propagation characteristics of chirped soliton in periodic distributed amplification systems with variable coefficients, Optik 123, (2012) 818-822

- [8] X. Zhang and X. Wang, Soliton propagation in birefringent optical fibers near the zero-dispersion wavelength, Optik 115, (2004)36-42
- [9] S. T. Cundiff, B. C. Collings, N. N. Akhmediev, J. M. Soto-Crespo, K. Bergman and W. H. Knox, Observation of Polarization-Locked Vector Solitons in an Optical Fiber, 82, 20 (1999)
- [10] Jing Huang and Jianquan Yao, Estimation of the fourth-order dispersion coefficient β4, Chinese Optics Letters, 10, 10, (2012)101903-101903
- [11] J. Sonesone, A. Peleg, Effect of quintic nonlinearity on soliton collisions in fibers, Physica D 195 (2004) 123-140
- [12] S. Konar, M. Mishra, S. Jana, The effect of quintic nonlinearity on the propagation characteristics of dispersion managed optical solitons, Chaos, Solitons and Fractals 29 (2006) 823–828
- [13] K. Porsezian, A. Hasegawa, V.N. Serkin, T.L. Belyaeva, R. Ganapathy, Dispersion and nonlinear management for femtosecond optical solitons, Physics Letters A 361 (2006) 504–508
- [14] A. M. Wazwas, Exact solutions for the fourth order nonlinear Schrödinger equations with cubic and power law nonlinearities, Mathematical Computer Modelling 43 (7–8) (2006) 802–808
- [15] A. Biswas, D. Milovic, Optical solitons in power law media with fourth order dispersion, Communications in Nonlinear Science and Numerical Simulation 14 (2009) 1834–1837
- [16] C. R. Menyuk, Nonlinear pulse propagation in birefringent optical fibers, IEEE Journal of Quantum Electronics, vol. QE-23, NO 2 (1987)
- [17] C. R. Menyuk, Stability of solitons in birefringent optical fibers. I: Equal propagation amplitudes, Optics Letters, 12, 8 (1987).



- [18] C. R. Menyuk, Stability of solitons in birefringent optical fibers. II: Arbitrary amplitudes, J. Opt. Soc. Am. B, 5, 2 (1988).
- [19] M. Mishra and S Konar, interaction of solitons in a dispersion managed optical communication system with asymmetric dispersion map, Journal of Electromagnetic Waves and Applications 21, 14 (2007) 2049-2058
- [20] M. Ekici, M. Mirzazadeh, A. Sonmezoglu, Q. Zhou, H. Triki, M. Z. Ullah, S. P. Moshokoa & A. Biswas,

Optical solitons in birefringent fibers with kerr nonlinearity by exp-function method, Optik, 131 (2016) 964-976

[21] P. Balla and G. P. Agrawal, Nonlinear interaction of vector solitons inside birefringent optical fibers, Physical Review A 98, 023822 (2018)

